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Tax Progressivity, Economic Booms and Trickle-Up Economics

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Abstract

We propose a method to decompose changes in the tax structure into orthogonal components measuring the level and progressivity of taxes. Similar to tax shocks found in the existing empirical literature, the level shock is contractionary. The tax progressivity shock is expansionary: Increasing tax progressivity raises (lowers) disposable income at the bottom (top) end of the income distribution by shifting the tax burden from the bottom to the top. If agents' marginal propensity to consume falls with income, the rise in consumption at the bottom more than compensates for the decline in consumption at the top. The resulting increase in output and consumption leads to rising capital gains for those at the high end of the income distribution that more than offsets their losses from higher income taxes. The net result is that an increasing progressivity leads to an increase in income inequality, contrary to what conventional wisdom might suggest. We interpret these results as evidence in favor of trickle up, not trickle down, economics.

JEL Classification: C32, C38, E62

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1 Introduction

Over the last 40 years, marginal tax rates for the top income brackets generally have fallen, resulting in a decline in income tax progressivity. The steady increase in income inequality over the same period has been well-documented [e.g., Alvaredo, Atkinson, Piketty and Saez (2013)]. Faced with increasing inequality, some suggest reversing the decrease in marginal tax rates for the highest income levels [e.g., Diamond and Saez (2011)]. While a literature has emerged to evaluate the optimal degree of progressivity of the tax system in theoretical models,[1] there remains a gap in the empirical regarding the impact of variations in income tax progressivity on the business cycle and inequality. In this paper, we provide a novel measure of progressivity that we then use to undertake such an empirical analysis, using minimal restrictions from economic theory.

A key difficulty in measuring changes in progressivity is that tax legislation typically contains a combination of both level and progressivity changes. Most empirical studies that evaluate the economic effect of changes in income taxes focus on changes to the *level* of taxes. Typically, these studies identify tax shocks using narrative evidence [e.g., Romer and Romer (2010)], the unexpected changes in the tax revenue series identified by a causal ordering [e.g., Blanchard and Perotti (2002)], or sign restrictions [e.g., Mountford and Uhlig (2009)]. While estimates of the magnitude of the tax-level multiplier vary across model assumptions, the general consensus is that increasing the level of taxes is contractionary.

The contribution of this paper is to determine how the variation in the tax burden across income levels affects economic outcomes. We develop a measure of income tax progressivity that is orthogonal to the level of taxes using data on the time-series variation of tax rates on different levels of wage income. Our empirical approach employs a factor-augmented VAR (FAVAR) using Bayesian methods, imposing priors from the literature on the term structure of interest rates to identify two factors: one that measures changes in the level of taxes and

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[1]Heathcote, Storesletten, and Violante (2017) and Feenberg, Ferriere, and Navarro (2017) both use quantitative heterogenous agent models, concluding that the current level of U.S. progressivity is optimal. However, Feenberg, Ferriere, and Navarro (2017) suggest that, if the labor supply choice is on the extensive margin only, optimal tax progressivity is much higher. In contrast, Kindermann and Krueger (2014) find that marginal tax rates as high as 90 percent can be justified. Sachs, Tsyvinski and Werquin (2020) argue that more progressive taxes can be justified if the tax code is suboptimal.

one that measures changes in progressivity.[2] To evaluate the effects of shocks to the tax factors, macroeconomic variables (e.g., output, consumption, hours, deficits, tax revenue and measures of income and consumption inequality) are included in the VAR with the tax factors.

The tax level factor is identified by assuming positive factor loadings for all tax rates—increasing the tax level increases tax rates across the board—and is analogous to the level factor from the literature on the term structure of interest rates. The tax progressivity factor, on the other hand, is identified by imposing that its loadings are strictly increasing with wage income, giving it a similar flavor to the slope factor in term-structure models. Thus, an increase in progressivity can be interpreted as a counter-clockwise twist in the "term structure of taxes," shifting the tax burden from low-income agents to high-income agents. To determine their effects on macroeconomic variables, we impose the additional identifying assumption that progressivity shocks are revenue-neutral on impact. This restriction allows us to disentangle progressivity shocks from the tax level shocks.

Our two factors account for, on average, over 80 percent of the variation of tax rates for incomes over $20,000. Consistent with the existing literature, we find that an increase in the level of taxes is contractionary. However, we also find a novel result that an increase in the progressivity of taxes is expansionary.[3] Expansionary tax progressivity shocks can result from heterogeneity in the workers' marginal propensities to consume. We hypothesize that lower-income workers are credit constrained with high marginal propensities to consume relative to higher-income workers. Thus, the increase in consumption and output resulting from reducing taxes on lower-income workers is not offset by the increase in taxes on high-income workers.

Not surprisingly, we find that progressivity shocks also have distributional effects. Because increasing progressivity shifts the tax burden from low to high incomes, one might anticipate

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[2]While the priors influence the estimated signs and magnitudes of the loadings, they remain loose enough as to not impose the type of exact restrictions found in the literature on the term structure of interest rates [e.g., Diebold and Li (2006)].

[3]The result that progressivity is expansionary is consistent with empirical work in Bachmann, Bai, Lee and Zhang (2017), who study the impact of fiscal volatility in a Krusell-Smith (1998) economy with heterogeneous agents and incomplete markets. They use the Castañeda, Díaz-Giménez, and Ríos-Rull (2003) tax function and make the progressivity parameter endogenous. They find that tax progressivity must be procyclical to match the data in the context of the model economy. While this is consistent with our empirical finding, the direction of causality differs between our two papers.

income inequality falling in response to a tax progressivity shock.[4] To the contrary, we find evidence that income inequality rises after an increase in progressivity.[5] One way to reconcile these results is that tax changes have both partial and general equilibrium effects. The positive progressivity shock that would lower inequality on impact can be offset by a subsequent response at the top end of the income distribution. We posit that high-income individuals—who typically own the majority of the capital—benefit more from expansions, sufficiently enough that it offsets their higher tax burden. The key for this explanation is that the change in progressivity is on *wage* income while inequality is measured with both *wage and capital* income.[6] While progressivity shocks have no real impact on the deficit-to-GDP ratio, increasing progressivity eventually increases tax revenue through an eventual expansion in output.[7]

To illustrate our intuition, we augment a simple two-agent New Keynesian (TANK) model from the class that Mankiw (2000), Gali, Lopez-Salido and Valles (2007), and Bilbiie (2008) develop with a fiscal authority that sets the degree of tax progressivity. One group of households, savers, have access to capital markets, while the other, nonsavers, are hand-to-mouth. To remain as close to the theoretical literature as possible, we use a Feldstein-type (1969) tax function, but allow the tax parameters to vary with the type of agent. This allows us to replicate the twist to progressivity from our empirical setting: marginal tax rates increase for savers while they decline for nonsavers. Such an increase to progressivity implies an expansion: nonsavers consumption rises, fueling an increase in aggregate output and consumption.

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[4]Progressivity's effect on inequality is actually theoretically ambiguous. The trade-offs from changing progressivity are described in Heathcote, Storesletten, and Violante (2017), who emphasize several channels by which tax progressivity can affect the economy. A progressive tax system may provide insurance against labor market uncertainty, lowering inequality. However, it also induces distortions to labor supply that reduce returns to working and can decrease investment in human capital, raising inequality. One of our objectives is to determine which of these effects dominates at the current level of U.S. progressivity.

[5]This result is robust to the measure of inequality—either a Gini coefficient or the spreads between income percentiles at the top and middle of the distribution.

[6]As documented by Piketty, Saez and Zucman (2018), capital income is the bigger driver of inequality, and tax rates on capital income are fairly flat. We also investigate the impact on consumption inequality, but our results are inconclusive.

[7]This result is consistent with the findings of Sachs, Tsyvinski, and Werquin (2020), who show that increasing tax progressivity in a Mirrleesian economy calibrated to the U.S. system raises government revenue. They refer to this finding as a "trickle-up" result for government revenue. We exploit time-series variation in taxes and revenues and find evidence that increases in progressivity have historically had such a trickle-up effect on government revenue.

Wage income increases for both types of households, as does capital income for savers. While income for all households increases, the gains imply an increase in income inequality.

The literature on tax progressivity is considerably smaller than the literature on overall tax changes. Moreover, studies that estimate the time series of tax progressivity changes in the U.S. are very limited. Most of these papers [e.g., Feenberg, Ferriere, and Navarro (2017; henceforth FFN) and a few others we discuss below] estimate annual tax progressivity by assuming a parametric tax function. Mertens and Montiel Olea (2018; henceforth MMO) study the effect of changes in average marginal tax rates (AMTRs) using a narrative approach similar to what Romer and Romer use for tax level changes. MMO identify a shock to the AMTR of the top one percent of the income distribution. They find that a counterfactual tax cut to this rate raises the incomes of the top one percent and temporarily raises GDP but has little effect on the income of the bottom 99 percent. This leads to an increase in inequality. At first glance, the MMO result might seem contrary to what we find. However, their exercise differs from ours in that: (i) we condition on changes to the level of taxes; (ii) we "twist" all tax rates, while they shock the tax rate for only a small slice of the income distribution; and (iii) their data uses only a few isolated events over the entire sample.[8] The second issue is important as MMO note that changes to the top marginal rate are unlikely to directly generate a large demand stimulus.

The balance of the paper is outlined as follows: Section 2 describes the data used to construct the tax factors, as well as the macroeconomic and inequality data used in the subsequent analysis. Section 3 describes the empirical model, the methods used to estimate it, and the prior used to identify the factor loadings. Section 4 discusses the empirical results using aggregate data, presents results using measures of inequality, and demonstates the main intuition with a simple TANK model. Section 5 conducts a counterfactual experiment that elucidates how changes in tax legislation manifest as changes in both level and progressivity factors. Section 6 summarizes the results and offers some takeaways.

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[8]We address the latter issue of the restricted sample in a series of robustness tests.

2 Data

Our objective is to determine the effect of tax progressivity shocks on a variety of macroeconomic and inequality data. To construct a measure of the distributional incidence of taxes, we need a measure of the time series of tax rates as a function of income. We also require the macroeconomic data of interest, data that will facilitate identification of the tax shocks, and the aggregate inequality data.

2.1 Tax Data

Many tax studies use aggregate government revenue, which is a single summary statistic of the total tax burden and omits its distributional effects. One possibility is to construct a measure of marginal tax rates by income brackets, which may initially seem straightforward. However, using tax brackets by themselves introduces a number of issues. First, the marginal tax rate is not a proper measurement of the final tax bill. Tax legislation often modifies deductions or exemptions rather than simply changing marginal rates. Second, the number of tax brackets and their associated incomes change over time. Third, the economic and demographic composition of the population can change over time.

Our data on tax rates are obtained from the TAXSIM model at the NBER for the years 1974-2015.[9] The TAXSIM program is essentially a tax bill computation program that uses a database of real individual-level tax returns obtained from the IRS to simulate the tax burden of the U.S. federal and state income tax systems. TAXSIM calculates tax liabilities and generates tables of aggregate statistics based on income measures. These tax rates apply to a hypothetical taxpayer who is married, has two dependents, and no itemized personal deductions.[10] The tax rates are based on an increase in the taxpayer's wage for a given current income.

We use the NBER table on U.S. Federal Marginal Income Tax Rates on Wage Income

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[9] These data are publicly available at http://users.nber.org/~taxsim/conrate/. The full dataset is available from 1960-2016. We use only data from 1974-2015 to match data availability for the inequality measures described in Section 2.3.

[10] The TAXSIM data do not solve all of the issues associated with the use of tax brackets. While the TAXSIM data do incorporate the EIC and standardized deductions for some dates, personalized deductions are omitted. Thus, the deductions associated with mortgage interest are also be omitted.

Data where income levels are expressed in real-1992 dollars based on the CPI-U price index. Data are available for tax rates on wage incomes at the following levels: \$5,000; \$10,000; \$20,000; \$40,000; \$100,000; \$200,000; \$400,000; and \$1,000,000. The tax rates for the first two levels of income are largely constant at 0 or negative numbers. To produce meaningful factors, we drop the \$5,000 and \$10,000 levels, leaving us with tax rates for six income levels to estimate two factors.[11]

The TAXSIM data contain time-series information on tax rates for a range of income levels. Our ultimate interest is in identifying tax shocks in a VAR and measuring the impact these shocks have on macroeconomic variables, as well as the distribution of income. To do this, we summarize the movements in the tax data by identifying two different effects.

First, we consider the overall level of taxes, similar to the exogenous tax shock evaluated in previous studies [e.g., Blanchard and Perotti (2002); Romer and Romer (2010)]. This level reflects the overall burden of taxes, where a rising level of taxes acts as a contractionary fiscal shock.

Second, we consider the progressivity of taxes, which determines how the tax burden is distributed across income levels. An increase in tax progressivity manifests as an increase in the taxes paid by higher-income levels and a decrease in taxes paid by lower-income levels. It is important to note that our interpretation of tax progressivity implies a shift in the tax burden across incomes that is orthogonal to changes in the level of taxes.

2.2 Macro Data

Our baseline case includes the two tax factors, the log of annual real GDP, and the log of annual real tax revenue for a sample period of 1974 to 2015. The revenue series is constructed as the log of current federal tax receipts converted to real terms using the GDP deflator. All of the macro data are annual and are obtained from the FRED database at the Federal Reserve Bank of St. Louis.

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[11] Omitting these two income levels from the estimation is equivalent to assuming that their tax rates are constant (perhaps fixed at zero). We verified the robustness of our results to excluding the two lowest income levels. These results are included in the Robustness Appendix.

We also estimate a number of variations of the baseline model that augment or replace real GDP as the macro variable of interest. These variations (a) replace real GDP with the log of real personal consumption, (b) include both real GDP and the log of total aggregate hours for nonfarm payrolls divided by the population 16 years and over, or (c) replace real GDP with the log of total capital expenditures.[12] Because changes in the level or progressivity of taxes may also affect the government surplus/deficit, we estimate an alternative model (d) that replaces federal revenue with the annual federal surplus/deficit as a share of GDP.

2.3 Inequality Data

To determine the distributional effects of progressivity shocks, we use Piketty, Saez and Zucman's (2018) data on income inequality. They combine tax return data from the IRS and data from the March Supplement of the Current Population Survey (CPS) to create a comprehensive estimate of income inequality. The CPS data is preferred to the tax data for the bottom end of the income distribution, where taxes are often not paid and returns are not filed. The tax data is preferred at the top end of the income distribution, where individuals in the CPS are anonymized by top-coding.[13] The new inequality measure combines both tax and survey data, making it more accurate than either dataset alone.

While many studies use on the income Gini, we focus on the gaps between the median income and higher income quantiles (90, 95, 99), as well as the difference between the 10th percentile and the 90th percentile. As pointed out earlier, the lower income quantiles pay little or no (and sometimes negative) taxes and would not directly affect the progressivity shock. Thus, we focus on the differences between high and median incomes, but include the 90-10 difference to verify that our results are robust to a broader measure of inequality.

To corroborate the mechanism for progressivity's effect on inequality, we consider five additional data series which capture the differential impact on those at the top end of the income distribution. The five series are: (i) aggregate capital gains income, (ii) capital gains

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[12]We replace GDP with consumption and investment because the two series are highly correlated. This is not an issue with hours, so in that case we include all five variables: tax level, progressivity, GDP, tax revenue, and hours.

[13]Atkinson, Piketty and Saez (2011) claim that the CPS data understate the rise in the top 1-percent of income.

income of the top 1% as a share of total income, (iii) capital gains income of the top 0.1% as a share of total income, (iv) the level of DJIA and (v) the level of the S&P500. To keep the models small (and because these series are highly correlated), we estimate the models with each series separately. Because these series are correlated with output, we replace output in the VAR with the series of interest. We use the same identification assumptions as used in the baseline VARs.

3 Empirical Approach

To determine how tax progressivity shocks affect the national economy, we utilize a FAVAR, where the tax factors are estimated jointly with the other model parameters in a state-space framework. This section outlines the model, identification, and inference.

3.1 Model

Let $R_t = [R_{1t}, ..., R_{Kt}]'$ be the $(K \times 1)$ vector of period-t (wage) income tax rates defined for K different income bins. Define τ_t as the period$-t$ value of the (latent) tax level factor and μ_t as the period$-t$ value of the (latent) progressivity factor.[14] The latent factors are related to the tax rates via

$$
\begin{bmatrix} R_{1t} \\ R_{2t} \\ \vdots \\ R_{Kt} \end{bmatrix} = \begin{bmatrix} \rho_1 \\ \rho_2 \\ \vdots \\ \rho_K \end{bmatrix} + \begin{bmatrix} \lambda_1^\tau & \lambda_1^\mu \\ \lambda_2^\tau & \lambda_2^\mu \\ \vdots & \vdots \\ \lambda_K^\tau & \lambda_K^\mu \end{bmatrix} \begin{bmatrix} \tau_t \\ \mu_t \end{bmatrix} + \begin{bmatrix} u_{1t} \\ u_{2t} \\ \vdots \\ u_{Kt} \end{bmatrix}, \tag{1}
$$

where the ρ_k are scalar intercepts, $u_t = [u_{1t}, ..., u_{Kt}]'$ and $E[u_t u_t'] = diag[\sigma_1^2, ..., \sigma_K^2]$ assumes that the only correlation in the tax rates arises from the factors. The λ_k^τ and λ_k^μ are factor loadings on the tax level and progressivity, respectively, that determine the relationship be-

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[14]We also estimated a three factor model, where the third factor can be interpreted as the curvature of taxes. As opposed to the term structure literature that restricts the third factor to be concave, the tax curvature should be convex (i.e., increasing more for higher incomes). We find that the mean responses are as predicted but insignificant. These results are in the Robustness Appendix.

tween the factors and the various tax rates. We discuss the importance of the factor loadings in more detail below.

Let X_t represent the $(N \times 1)$ vector of variables of interest and define $Y_t = [\tau_t, \mu_t, X_t']'$. Then, the specification of the aggregate-level structural VAR is:

$$A_0 Y_t = A(L) Y_{t-1} + e_t, \tag{2}$$

where A_0 is the matrix of contemporaneous effects, $A(L)$ is a matrix polynomial in the lag operator, and $e_t \sim N(0, I)$ are the structural shocks. To facilitate exposition in the section outlining the structural identification below, we can rewrite (2) as

$$
\begin{bmatrix} A_{0,\tau\tau} & A_{0,\tau\mu} & A_{0,\tau x} \\ A_{0,\mu\tau} & A_{0,\mu\mu} & A_{0,\mu x} \\ A_{0,x\tau} & A_{0,x\mu} & A_{0,xx} \end{bmatrix} \begin{bmatrix} \tau_t \\ \mu_t \\ X_t \end{bmatrix} = \begin{bmatrix} A_{\tau\tau}(L) & A_{\tau\mu}(L) & A_{\tau x}(L) \\ A_{\mu\tau}(L) & A_{\mu\mu}(L) & A_{\mu x}(L) \\ A_{x\tau}(L) & A_{x\mu}(L) & A_{xx}(L) \end{bmatrix} \begin{bmatrix} \tau_{t-1} \\ \mu_{t-1} \\ X_{t-1} \end{bmatrix} + \begin{bmatrix} e_t^\tau \\ e_t^\mu \\ e_t^x \end{bmatrix},
$$

which isolates the effects of lags of variable j on variable i in each lag polynomial, $A_{ij}(L)$.[15]

One could imagine the relationship between tax progressivity and macroeconomic outcomes is nonlinear. For example, the effect of a productivity shock on output may depend on the distribution of income. We view our model as a first-order approximation of this more general nonlinear model, where results are obtained under the assumption that changes in progressivity and the income distribution are local to their initial conditions (i.e., relatively small).

3.2   Identification

Our model presents two types of identification issues discussed below.

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[15] We incorporate a linear trend into the VAR.

3.2.1 Factor Identification

The first issue requires imposing restrictions on the factor loadings to identify the factors. As we implied above and will discuss again in detail later, most tax legislation will be represented by a combination of both level and progressivity shocks, where the loadings determine the effect of a unit change in the corresponding tax factor on the various tax rates. As described previously, we impose that (i) $\lambda_k^\tau > 0$ for all k and (ii) $\lambda_m^\mu \geq \lambda_k^\mu$ for $m > k$. The former set of restrictions implies that raising the level of taxes increases tax rates across the board.[16] The second restriction implies that increasing tax progressivity raises the tax rate more as income increases. Note also that λ_k^μ need not be strictly positive; in fact, in practice, λ_k^μ will be negative for low income levels. This implies that $\sum_k \frac{\lambda_k^\tau}{K} \tau_t$ represents the (unweighted) average level of taxes across all incomes and $\lambda_k^\mu \mu_t$ raises (or lowers) the income-dependent tax level from the average.

These restrictions identifying the loadings differentiate our model from the parametric tax function outlined in Feldstein (1969) often used in the literature [e.g., in FFN and others].[17] First, the parametric tax function implies an equal increase in tax rates across all incomes for a given increase in the level, implying $\lambda_i^\tau = \lambda_j^\tau$ for all i, j. Moreover, the parametric tax function implies the difference between tax bins is monotonically increasing with income; the restrictions on our estimated loadings imply that only the rates are monotonically increasing with income.

The use of the parametric tax function is analogous to the "functional VAR" that Inoue and Rossi (2019) propose to measure the effects of monetary policy. Inoue and Rossi identify composite shocks to the level, slope, and term structure of interest rates by examining the evolution of the parameters in Nelson-Siegel regressions. In our model environment, the Nelson-Siegel-type (1987) factors could be recovered by imposing $\lambda_k^\tau = 1$ for all k and $\lambda_{k+1}^\mu > \lambda_k^\mu$ for all $k = 1, ..., K - 1$. Similarly, an approximation of principal components would impose

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[16]Our restriction allows the effect of tax level shocks to vary across income brackets. We also estimated a more restricted model in which the loadings on the tax level are all set to 1 in the spirit of Reis and Watson (2010). Results were qualitatively similar and are reported in the Robustness Appendix.

[17]FFN construct progressivity using a nonlinear tax function based on Feldstein (1969), $\tau(y) = 1 - \lambda y^{-\gamma}$, where $\tau(y)$ is the tax rate on the level of income y. The parameter γ in their scheme represents tax progressivity.

$\lambda_k^\tau \simeq 1$ for all k, but would not strictly hold to 1, and the upper block of the variance-covariance matrix of the state equation would be diagonal.

3.2.2 Shock Identification

The second identification issue involves identification of the structural tax level and progressivity shocks in the VAR [for an overview of these issues, see Ramey (2016)]. While many methods have been proposed to identify fiscal shocks in VARs (e.g., narrative, recursive, exclusion, sign restrictions, etc), there are no well-established methods of disentangling the tax level and progressivity shocks. In our case, the nature of the economic question and annual frequency of the data dictate our choice of the method of identification.

Two of the other empirical papers in the literature are MMO and FFN. MMO identifies their shocks using narrative methods, but focuses on a subset of tax rates and legislative events. FFN constructs a tax progressivity series, but they do not evaluate the effects of progressivity shocks in a VAR. Mountford and Uhlig (2009) identify fiscal shocks using the sign restriction approach of Uhlig (2005). In their case, economic theory provides unambiguous restrictions that can identify their revenue and spending shocks. In contrast, there is no established theoretical result to identify pure progressivity shocks, leading us to take an agnostic route and establish a set of stylized facts. Moreover, the sample and frequency of the data impose limitations on the size of the VAR, hindering the use of sign restrictions.

We identify the structural form of the VAR using *non-recursive* exclusion restrictions on the matrix of contemporaneous effects. To disentangle the two different tax shocks, the key identifying restriction—as we have discussed above—is that tax level shocks directly affect revenue contemporaneously, while tax progressivity shocks do not.[18] Thus, the (positive) progressivity shock is a revenue-neutral (counterclockwise) twist in the "term structure" of tax rates resulting in a reallocation of the tax burden.[19] Our identifying assumptions imply that changing a subset of the tax rates likely results in a combination of both tax level and

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[18] These identifying assumptions result in a third difference between our model and the FFN model that uses the tax function. A shock to the progressivity parameter in the tax function is not revenue neutral. Thus, the interpretation of the two progressivity shocks would be different.

[19] Our assumption is that progressivity does not affect revenue directly but, within the year, can affect revenue through a change in output.

progressivity structural shocks. The experiment in Section 5 below highlights this.

To complete our set of identifying restrictions, we assume that the tax level and tax progressivity shocks are contemporaneously uncorrelated. While we allow both tax shocks to affect the macro variables (with the exception of our key identifying restriction), we rule out contemporaneous feedback from the macro variables to taxes.[20] In particular, our identifying assumptions on the baseline specification impose the following structure on A_0:

$$A_0 = \begin{bmatrix} a_{\tau\tau} & \mathbf{0} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & a_{\mu\mu} & \mathbf{0} & \mathbf{0} \\ a_{\tau Z} & a_{\mu Z} & a_{ZZ} & a_{TZ} \\ a_{\tau T} & \mathbf{0} & a_{ZT} & a_{TT} \end{bmatrix},$$

where $X_t = [Z_t, T_t]$ with Z_t the log of real GDP and T_t the log of real tax revenue.

3.3 Inference

We estimate the FAVAR described above at the annual frequency with two lags using Bayesian techniques. Estimating parametric factors—rather than principal components—allows us to impose restrictions on the factor loadings that will produce more economically-interpretable factors.[21] The form of the prior we impose is relatively standard. The ρ_k are obtained by ex ante demeaning the tax series and do not require a prior; similarly, we demean the macro variables in the VAR. The variances of the tax rates are inverse gamma priors and assumed to be independent, and the factor loadings have normal priors. The prior parameters are shown

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[20] Our identification is consistent with block recursive ordering, where the factors are ordered first, with the additional restrictions that (i) the progressivity shock does not affect revenue and (ii) that the two tax shocks are orthogonal. In a previous version of the paper, we produced impulse responses for shocks identified using the Cholesky identification. The results were qualitatively similar and are in the Robustness Appendix.

[21] In the term-structure literature, factors are often generated by methods that restrict the loadings on the factors—see, for example, Nelson and Siegel (1987). In that paper, the level factor is estimated assuming coefficients on the factor are all unitary. The yield curve then rises equally across all maturities with movements in this factor. The slope factor imposes rising coefficients across maturities, with a free parameter to govern the slope. The movements in the slope factor then have heterogeneous effects on yields. Their approach does not impose orthogonality in the two factors as would be imposed in principal components. The state-space framework allows us to parameterize a prior that puts ex ante weight on a zero correlation between the two factors as in the principal components approach while allowing priors to push the loadings towards those in the term-structure literature.

in Table **1**.

The FAVAR is estimated with a Gibbs sampler, a Markov-chain Monte Carlo technique. Start with an initial draw of the parameters and the factors. We then sequentially draw from one block of parameters, conditional on the last draw of the other blocks and the data. After allowing for a suitable number of draws to allow the algorithm to converge, draws from the conditional distributions reflect draws from the joint posterior density. For our sampler, we have three blocks: (1) the VAR parameters, (2) the factors, and (3) the measurement equation parameters. Conditional on the factors, we estimate the VAR in the structural form using a sampler described in Waggoner and Zha (2003).[22] We then obtain the reduced-form parameters from:

$$Y_t = B\left(L\right)Y_{t-1} + \varepsilon_t, \tag{3}$$

where $B\left(L\right) = A_0^{-1}A\left(L\right)$, $\varepsilon_t \sim N\left(0, \Omega\right)$ are the reduced-form shocks, and $\Omega = A_0^{-1}A_0^{-1\prime}$ is the reduced-form variance-covariance matrix. The factors are drawn from the smoothed Kalman filter posteriors using the reduced-form VAR parameters for the state equation. For this draw, we impose the additional identifying restrictions discussed above that the loadings on the first factor are positive and the loadings for the second factor are increasing across the income levels.[23,24] Draws from the third block are conjugate normal–inverse-gamma.

4   Results

4.1   The Tax Factors

Before we consider how different types of tax shocks affect aggregate economic outcomes, we examine some of the properties of the tax factors obtained from the FAVAR. We model

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[22] A brief overview of the prior and the sampler is provided in the Appendix.

[23] The factors from the state-space model depend on the VAR specification. Principal components analysis (PCA) produces similar tax factors for the baseline model. The correlation between the level (progressivity) factors obtained from these two methods is 0.97 (0.69). Despite the model dependency, we prefer the structure of the FAVAR, as it allows us to impose further identifying restrictions on the factor loadings.

[24] The income brackets at the high end ($400k and $1M) are wider than at the low end ($20k, $40k, and $100k). Consequently, the prior on the progressivity loadings are slightly increasing for the top two brackets.

changes to the tax code similarly to how one would model changes in the term structure of interest rates, thereby reducing the dimensionality of the tax rate data by summarizing their movements into the two latent factors plotted in Figure **1**.

Figure 1: Tax factors from the FAVAR

Our tax factors are consistent with the tax series found in other studies. For example, the correlation between the difference of the tax level factor and the Romers' tax shock series (for 1974-2007, dates in which the series overlap) is 0.22. The progressivity factor exhibits a sharp decline in the late 1980s followed by a steady increase, consistent with narrative evidence and with the progressivity series computed from a parametric tax function in FFN. The correlations between changes in our progressivity factor and changes in the marginal tax rates across brackets are consistent with our interpretation of progressivity. For the three lowest brackets, these correlations are negative and range from -0.04 at \$20,000, to -0.10 at \$40,000, to -0.08 at \$100,000. Alternatively, the correlations are positive for the three highest brackets, ranging from 0.27 at \$200,000, to 0.44 at \$400,000, to 0.40 at \$1,000,000. Thus, while the top rate alone clearly matters for progressivity, our measure differs from this simple measure in capturing twists in the entire tax code.

Table 2: Variance Decompositions from the FAVAR

How well do these factors represent actual fluctuations in the tax rates? Table **2** shows the shares of the variance of each tax bracket explained by the two tax factors. Taken together, the level and progressivity factors explain, on average, over 70 percent of the tax data for the income brackets in our sample. These results suggest that our factor approach provides a parsimonious, yet comprehensive, characterization of movements in taxes.

Movements in the factors can also be associated with historical policy changes reflected by the vertical lines in Figure **1**. For example, in the early 1980s, the Kemp-Roth Tax Cut called for an across-the-board decline in marginal tax rates in an effort to boost the economy.

This tax cut manifested more in a gradual decline in the overall level of taxes (the first factor) but a less substantial change in progressivity. On the other hand, the Reagan Tax Reform Act of 1986, which was meant to simplify the tax code by eliminating a large number of tax brackets, led to a substantial decline in both factors. The Omnibus Budget Reconciliation Act of 1990 increased the top marginal tax rate from 28 percent to 31 percent, reformed capital gains taxes, and limited high-valued itemized deductions. Subsequent to this legislation, the level of taxes do not change substantially but progressivity rises.

These historical episodes highlight the importance of modeling both changes in the level of taxes and changes in the progressivity of taxes. While each piece of legislation affected the level of taxes, without simultaneously modeling tax progressivity, the total impact of the change in the tax law may be misinterpreted, if not mismeasured.

4.2   The Effect of Tax Shocks on Tax Rates

Figure 2: Factor Loadings

We now consider the static effect of a unit change in the two tax factors on the tax rates for each income level as reflected in the factor loadings. From equation (1), we can obtain the average change in the tax rates at the time of a change in either the level or progressivity.

Figure **2** plots the factor loadings for the two estimated tax factors as a function of income. Two results are immediately apparent. First, the loadings on the tax-level factor are all positive—ranging between 0.2 and 1.9 and averaging 1.1. However, they are not equal across income levels nor are they monotonically increasing. A unit shock to the tax-level factor results in an increase in the tax rate of about 0.4 percentage points at $40,000 but 1.0 percentage points at $100,000. Thus, an increase in the tax-level factor will produce an across-the-board, yet not equally-distributed increase in tax rates across all income levels.[25]

Second, the loadings on the progressivity factor are negative for low incomes and positive for higher incomes. Thus, an increase in the progressivity factor shifts the tax burden

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[25]As a robustness check, we estimated a model in which the loadings on the level factor were restricted to be equal across incomes and fixed at 1. The resulting progressivity factor was qualitatively similar and are reported in the Robustness Appendix.

unequally across income brackets. In particular, the twist in the tax term structure places increased tax burden only on the top three rates, with only a small increase in the lowest of these three top rates. This result is not surprising given that our prior also has increasing means across incomes and that we require a shock to the factor to be revenue neutral. However, the point values of the posteriors can differ substantially from the prior mean; for example, the prior mean at \$100,000 is 0 but the posterior mean is -1.2.

4.3 Macroeconomic Outcomes

Having determined how shocks to the tax factors affect the tax rates, we now turn to evaluating the effect of the tax shocks on macroeconomic outcomes. To do this, we compute the impulse responses of the macro variables to the two tax shocks, identified by the restrictions described above.

Figure 3: Benchmark Impulse Responses

The eight panels of Figure **3** plot the impulse responses to the tax level (top row) and progressivity (bottom row) shocks. Consistent with the existing literature, the tax-level shock is contractionary, increasing revenue on impact but eventually lowering revenue via the economic contraction. The bottom row of Figure **3** reports the effects of a positive progressivity shock. An increase in progressivity *raises* output over a 5-year horizon—that is, shifting the tax burden from the relatively low income to the relatively high income results in an economic boom. While we assume that progressivity has no direct effect on revenue, it can indirectly have an effect within the first year through the subsequent rise in output.

Changes in the level or progressivity of taxes can, in theory, have effects on government revenue. The response of government revenue to the progressivity shock in Figure 3 is positive and significant. This result is consistent with Sachs, Tsyvinski, and Werquin (2020), who show that an increase in tax progressivity in a calibrated Mirrleesian economy raises government revenue. They refer to this finding as a "trickle-up result" for government revenue. Here, we document the empirical response of government revenue using time-series data with little

economic theory. As Sachs, Tsyvinski and Werquin (2020) argue, the trickle-up result implies significant issues with the current general equilibrium approach to optimal tax theory.[26]

Figure 4: Alternative Measures of Economic Activity Impulse Responses

These results are consistent with several variations of the baseline model that augment or replace real GDP as the macro variable of interest. Figure 4 shows the responses of three alternative measures: consumption (first column), hours (middle column), and capital expenditure (right column). These are all obtained from separate aggregate-level VARs for the sample 1974 to 2015 in which we replace output with consumption or capital expenditure or add hours to the VAR with output.[27] In all cases, the increase in progressivity consistently produces an economic expansion: output, consumption, hours worked, and capital expenditure all rise.

Figure 5: Benchmark and Purely Exogenous Impulse Response Functions

The expansionary effect of increasing progressivity is a striking result. Thus, it is important to verify its robustness to alternative identification schemes, as there are competing views on how to best identify a structural shock. For example, in the monetary literature, Coibion (2012) investigates the reasons for differences between Romer and Romer (2004) monetary shocks and monetary shocks identified with the Cholesky decomposition. In the spirit of that exercise, we construct a set of alternative progressivity shocks from our progressivity series, but we use only the observations occurring on the MMO dates. In this sense, we "filter" our full-sample shocks and employ only the exogenous events that they consider.[28] Figure **5** shows the result of this exercise. From the results shown in the top row, it is clear that results from the unfiltered sample and the results using only the MMO dates are qualitatively

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[26] Results including the deficit are qualitatively similar and are discussed in the Robustness Appendix.

[27] For the VAR with output and hours, we retain the restrictions from the previous A_0 above and impose the additional restriction that an hours shock does not affect GDP or the tax factors on impact.

[28] They include fifteen events in their sample from 1946-2012, with eleven of their events occurring in our sample period of 1974-2015.

similar, although there are some differences in magnitudes. Importantly, in the second row, the response of GDP to each shock is consistent with our benchmark results.[29]

The expansionary effect after an increase in progressivity is a new empirical result that is uncovered by our methodology for measuring tax progressivity shocks. The result is consistent with papers that find heterogeneous responses of consumption to changes in income [e.g., McCarthy (1995); Dynan, Skinner, and Zeldes (2004); Jappelli and Pistaferri (2010); and Parker, Souleles, Johnson, and McClelland (2013)]. Further, Gruber and Saez (2002) find that, because high earners can itemize deductions, the elasticity of taxable income varies across the income spectrum. In particular, agents at the low end of the income distribution are credit-constrained and wish to consume more. As their tax rates fall, assuming that their marginal propensity to consume is near one, they increase their consumption nearly dollar-for-dollar. Those at the higher end of the income distribution have lower marginal propensities to consume and do not reduce their consumption as tax rates rise. Additionally, changes to marginal tax rates for the wealthy appear to have little impact on work effort.[30] The expansion also leads to an increase in aggregate hours worked.

4.4 Progressivity Shocks and Inequality

The effect of a tax progressivity shock on income inequality can be decomposed into two parts: a partial-equilibrium impact effect and the subsequent multiplier effect. Intuitively, the impact effect lowers inequality by increasing the marginal tax rate for high-income individuals and decreasing it for low-income individuals. The subsequent propagation effect is related to the economic boom caused by the increase in progressivity. If, for example, low- or middle-income wages rise as hours worked increase and labor market conditions tighten, we could see a further decline in inequality. On the other hand, if corporate profits rise in response to

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[29]The tax-level factor falls following an increase in progressivity. To ensure that this is not responsible for the subsequent economic boom, we estimate a restricted VAR such that each factor depends only on its own lags: $A_{\tau\mu}(L) = A_{\mu\tau}(L) = A_{\tau x}(L) = A_{\mu x}(L) = \mathbf{0}$. Increasing the tax level remains contractionary and increasing progressivity remains expansionary. Under these restrictions, the contractionary effects of level shocks are larger and the expansionary effects of progressivity shocks are delayed. These results are available from the authors upon request.

[30]See, for example, Zidar (2019), who considers income heterogeneity by location and finds that tax cuts for the top 10% have very small effects on employment growth in that demographic.

increased output and wages are stagnant, we could see an increase in inequality since capital ownership is concentrated at the top end of the income distribution.

Figure 6: Income Inequality IRFs

Using the Piketty, Saez and Zucman's (2018) data on income inequality, we consider the difference between log income levels at various percentiles: 99-50, 95-50, 90-50, and 90-10. These measures provide a thorough depiction of how the income differential is changing across various levels within the overall distribution. We find that income inequality rises after the progressivity shock (see Figure 6).[31] This increase in income inequality, however, does not necessarily imply that those at the lower end of the distribution are less well-off in terms of welfare: The expansion increases their income and consumption, but the income of those at the top end of the distribution increases more.[32] Of the four inequality measures depicted in Figure 6, we see the strongest response in the changes of the 99-50 percentile and the 95-50 percentile: Those at the top gain much more than those in the middle during the expansion. Moving further into the middle of the distribution, the change for the 90-50 percentile is smaller but still significant, suggesting that the increased Gini is driven by the large gains of the upper tail. At the lower end of the distribution, the changes in the 90-10 percentile suggest an even smaller and insignificant effect on inequality on impact. This may capture stagnation in the lower-income individuals that may not experience substantial gains relative to higher-income owners of capital.

Trickle-down economics suggests that lowering tax rates on those with high incomes spurs an expansion. In contrast, our empirical results suggest that the opposite is true. Lowering the tax burden on lower incomes sets off an expansion that also raises the incomes of those at the high end of the income distribution. This is consistent with trickle-up—not trickle-down—economics. This result can be understood by considering the fact that the change

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[31] When adding a measure of inequality to the VAR, we replace output and impose the baseline identifying restrictions on A_0.

[32] This result is consistent with empirical evidence that the economy disproportionately and increasingly rewards those at the top end of the distribution. It is also consistent with stagnant wages in the middle of the income distribution, which has occurred even in expansions. See for example, Saez and Zucman (2020) for recent evidence on the increasing share of income of the top one percent.

in progressivity is on wage income while income inequality is measured with both wage and capital income. Our income inequality data is from Piketty, Saez and Zucman (2018), who argue that capital income is a greater driver of income inequality than wage income. They also argue that inequality is being driven by the upper tail of the distribution, which is consistent with our interpretation of the results.

To further examine the story regarding capital incomes rising for those at the top, we consider several measures which capture this dynamic: (i) aggregate capital gains income, (ii) capital gains income of the top 1% as a share of total income, (iii) capital gains income of the top 0.1% as a share of total income, (iv) the level of DJIA and (v) the level of the S&P500. The anticipated response of each of these variables under our hypothesized mechanism is positive—that is, a tax progressivity shock that increases income inequality through rising capital values should increase capital gains income and increase stock prices. Figure 7 collects the impulse responses for the five variables (obtained from separate VARs) to tax level (top row) and progressivity (bottom row) shocks. We find a significant increase in all but one of the variables of interest to an increase in progressivity.[33] This suggests that an increase in progressivity leads to a rise in income that, in turn, leads to an increase in capital gains income and stock prices. While we do not take these results as explicit proof of our proposed mechanism, they are consistent with our argument.

Figure 7: Capital Gains, Capital Income, and Stock Market IRFs

To summarize, we find that increasing the progressivity of taxes raises GDP and income inequality. We previously hypothesized that a shock to progressivity acts initially through the consumption channel. An increase in tax progressivity raises disposable income for low-income agents and lowers disposable income for high-income agents. This, in turn, raises consumption at the low end of the income distribution and lowers consumption at the high end of the income distribution. To generate a net increase in aggregate income, consumers at the low end of the income distribution spend all or most of their newfound income, while

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[33]The S&P500 does increase as well but the response is insignificant. We see an analogous, insignificant decline in this series following an increase in the tax level.

consumers at the high end of the income distribution reduce their consumption by only a (perhaps small) portion of the decrease in disposable income.[34]

The textbook tax multiplier story does not imply an increase in income inequality. In the single (type) agent model, a shock to the tax rate that increases disposable income generates a multiplier effect in which the increase in consumption is repeatedly redistributed back to the agents. In the heterogeneous income environment, if this multiplier income is proportionately redistributed across both high- and low-income agents, the Gini does not change.[35] However, if high- and low-income agents supply differentiated labor and the flexibility of wages varies with the labor type, the proportionate redistribution is broken, and income inequality can increase. We illustrate this idea next with a simple model.

4.5   Progressivity Shocks in a TANK Model

So far, we have posited transmission channels that can account for our results. We now present a simple heterogeneous agent New Keynesian model with two types of agents [Mankiw (2000); Gali, Lopez-Salido and Valles (2007)] and show that the channels we emphasize imply an expansion following an increase in tax progressivity that is coupled with a rise in income inequality. In the model, "savers" have access to capital markets, and "nonsavers" live hand-to-mouth. As such, nonsavers have a higher marginal propensity to consume. Each type of household supplies a distinct labor service [Bhattarai, Lee and Yang (2023)] and has some monopoly power in the wage setting. The government taxes wage income, and the rate is increasing in the level of income. Firms use both types of labor, combined with a capital stock, for production. The remaining features are standard in a New Keynesian model: firms and households are subject to frictions when adjusting their prices/wages, the central bank follows a Taylor rule, and Ricaridan equivalence holds.[36]

To stay closely aligned with the theoretical literature, we adopt a Feldstein-type (1969)

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[34]This result contrasts with Kindermann and Krueger (2014), who find that aggregate consumption falls with a rise in the highest marginal tax rate. However, as they note in their paper, their results depend on assumptions about the labor productivity process and elasticities. Here, we provide a set of empirical facts independent of such assumptions.

[35]Moreover, a lump-sum–type redistribution would lower the Gini, as it would raise incomes at the low end of the income distribution proportionately more.

[36]Full details about the model and its benchmark calibration are included in the Appendix.

tax function, but allow its parameters to vary by household type. Specifically, we assume a homogeneous tax function in the steady state and consider a shock that raises the progressivity parameter on savers while simultaneously lowering the same parameter for nonsavers, ensuring revenue neutrality. This flexibility enables us to capture the key feature observed in our empirical setting: marginal tax rates rise for savers but decline for nonsavers.

Figure 8 plots the impulse responses following our policy experiment. By design, the policy increases the average and marginal tax rates of savers. Revenue neutrality implies a twist to the tax schedule as average and marginal rates of nonsavers decline. Nonsavers consume more with the increase in their disposable income, while the higher tax rate to savers causes them to lower their consumption (not pictured). In the aggregate, the effect from nonsavers dominates, leading to an increase in aggregate consumption. To meet the increased demand for their goods, firms increase demand for labor, resulting in more hours worked by both savers and nonsavers. The wage income for both agents increases on impact, but wage rigidities imply that the changes occur in disproportionate amounts. Higher demand for capital increases its rental rate, fueling an expansion in capital income as well. The last panel of figure 8 plots the log difference in savers' and nonsavers' income. Overall, savers' income increases more than that of nonsavers, increasing the level of inequality.

While our quantitative model incorporates several standard real and nominal frictions found in the literature, it remains a stylized framework when it comes to capturing changes in the distributional structure of income taxation. Given this limitation, it is perhaps unsurprising that the model falls short in replicating the persistence observed in our empirical findings. Rather, the model is intended to illustrate the key mechanisms driving the transmission of a tax progressivity shock.

4.6 Robustness

In the previous sections, we noted in footnotes that our results are robust to alternative identifications of shocks, restrictions on factor loadings, measures of economic activity, the number of tax brackets used, and the number of factors estimated. Our final measure of

robustness is to examine the assumption that the model parameters are stable over time. It may be the case that the relationship between taxes and income varies with structural changes in the economy. To investigate this, we re-estimate the model allowing for a break in the progressivity factor loading coefficient over three periods: (i) 1992, after the Reagan tax cuts and before the Clinton tax policies; (ii) 1984, ending with the start of the Great Moderation; (iii) 2007-2015, the Great Recession period. Note that we re-estimate the model allowing for one break at a time.

We find that the estimated factors are very highly correlated when allowing for a break. This result is somewhat expected as both Del Negro and Otrok (2008) and Bates, Plagborg-Moller, Stock and Watson (2013) find that estimates of factors are robust to time variation in parameters or structural instability. Additionally, the impulse response functions are very similar when allowing for breaks. These results are left to the Robustness Appendix as they are very similar to the results we report in the main text.

5   Raising Marginal Tax Rates: An Experiment

In the previous sections, we showed that increasing the level of taxes is contractionary while increasing the progressivity of taxes is expansionary. As Figure **2** suggests, most of the tax policies enacted over the sample period are a combination of shocks to both level and progressivity. For example, we highlighted earlier that the Reagan Tax Reform Act of 1986 resulted in a decline in both factors. While the effect of the level and progressivity shocks can be evaluated in isolation in the VAR, the mapping between a real-world tax policy and the change in the level and progressivity shocks occurs in the measurement equation of the factor model. Thus, to determine the net effect of tax policies that comprise both a level and a progressivity shock, we must evaluate how a particular policy maps into the two factors.[37]

Here, we consider two examples of tax policies, both of which would be considered contractionary in an environment where the tax level was the only policy instrument. We describe

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[37]As noted in footnote 14 we also estimated a 3 factor version of the model. In principle, this would allow for different sets of policy options to hit a target. Since the curvature factor was not significant, we do not pursue these policies here.

how the changes in legislation map into the factors and evaluate their net effects.

At time T, the update step of the Kalman filter determines the magnitude of the change in the mean of the posterior distribution of the state vector. Thus, the effect of changing any part of the tax rate vector, R_T, on F_T would be proportional to the Kalman gain, G_T:

$$\Delta F_T = G_T^* \Delta R_T,$$

where G_T^* represents the first two rows of the Kalman gain matrix. Note that this decomposition imposes that the largest percentage of the variance of R_T is explained by the factors. The balance of the variance is remanded to the innovation in the measurement equation, which we assume does not propagate through the VAR and, thus, does not affect output.

Our first experiment considers proposed tax legislation that increases the tax rate on the top of the income distribution by 10 percentage points. In our model, this tax legislation is represented by an increase in R_{KT}, where $K = \$1$ million and T is the time at which the tax increase is levied. Specifically, the proposed tax legislation can be modeled as

$$\Delta R_T = \left[\mathbf{0}'_{[(K-1) \times 1]}, \Delta R_{KT} \right],$$

where $\Delta R_{KT} = 0.1$. Given this counterfactual change in the tax code, we can compute the effect on the factors.

Based on the means of the posterior distribution of the model parameters, the proposed tax legislation results in a change in the factors of $\Delta F_{1T} = -0.0003$ and $\Delta F_{2T} = 0.0002$. Thus, the proposed legislation acts to shift down the level of taxes, but increase progressivity. Given these changes in factors, we can compute the net effect of the tax legislation assuming that ΔF_T embodies a reduced-form shock. We want to isolate the effects of the policy change via transmission through changes in tax level, progressivity, and then a composite of the two shocks. Given $\Delta F_T = [\varepsilon_t^\tau, \varepsilon_t^\mu]'$, we obtain the vector of structural shocks from the reduced-

form effects as follows:

$$\begin{bmatrix} e_t^\tau \\ e_t^\mu \\ e_t^x \end{bmatrix} = A_0 \begin{bmatrix} \varepsilon_t^\tau \\ \varepsilon_t^\mu \\ 0 \end{bmatrix}.$$

We isolate the effects of e_t^τ and e_t^μ individually and then consider the net effect of a composite of the two structural shocks.

The top row of Figure **9** shows the effect of the composite shocks. The left panel shows the impulse response of output to a level shock of the appropriate size; the center panel shows the impulse response of output to a progressivity shock of the appropriate size; and the right panel shows the net effect, represented by the sum of the two components. Both a decrease in the level of taxes and an increase in tax progressivity are expansionary. Thus, the long-run net effect of the legislation shown in the right-most panel is unambiguously expansionary in our framework. In a model in which the tax level was the only instrument, the legislation would be an increase in the tax level and, thus, unambiguously contractionary.

Figure 9: Experiment 1/2

Figure 10: Graphical Depiction of the Experiments

What leads to the difference in the results across the two models? While the model with just the level shock can only produce the proposed legislation with a contractionary increase in taxes, the left panel of Figure **9** shows how this legislation manifests in our environment. Each of the tax rates are the sum of a tax level component and a tax progressivity component. The increase in the highest tax rate leads to a counterclockwise rotation in the distribution of taxes—an increase in tax progressivity. The increase in tax progressivity alone would increase the expected tax rates at incomes just below $1 million (i.e. $200k and $400k). Thus, to compensate for the increase in these rates caused by the increase in progressivity, the tax level decreases.

We next consider a 10-percentage-point increase in each of the top two tax rates (at $400k and $1M income). This legislation produces both an increase in the level of taxes ($\Delta F_{1T} = 3.53$) and the progressivity of taxes ($\Delta F_{2T} = 0.71$). The right panel of Figure **10** shows why this legislation produces an increase in the level of taxes. To capture the rise in the top two rates, progressivity increases even more than in the previous counterfactual. The expected rates at the lowest incomes are now too low and the tax level must shift up to account for this.

Because one effect is contractionary and one effect is expansionary, we need to compute the net effect to determine whether the sign of the response is positive or negative. The bottom row of Figure **9** shows the effect of each shock and the combined effect (right panel). Here, the level effect dominates the progressivity effect and produces a net negative effect on output in the long run.

6   Summary and Conclusion

The objective of this paper is to develop a set of empirical facts related to changes in the progressivity of taxes. To do so, we developed a new measure of revenue-neutral progressivity that conditions on changes in the level of taxes. The impact of our tax-level factor is consistent with the existing tax literature and most economic theory. Our progressivity factor yields novel empirical insights. In particular, we find evidence in favor of trickle-up economics. After an increase in progressivity, an economic boom begins. Paradoxically, the boom does not lower income inequality because those in the upper tail of the distribution benefit more from the economic gains. Qualitatively similar responses to innovations in tax progressivity can be obtained from a TANK model with both savers and nonsavers. We do not interpret this as a negative result; rather it suggests that other, non-income-tax-based policies would need to be enacted to reduce inequality.

A key message of the paper in evaluating policy is that because taxes are levied on people differently and there is heterogeneity in the response to taxes across the income distribution, one needs to evaluate the effect of any tax legislation by considering both the level of taxes and

the degree of progressivity. In models where only the level shock is available, some legislation would be considered contractionary. In an environment where both level and progressivity are relevant, the effect of the same legislation might be ambiguous until one examines the relative changes in both level and progressivity.

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Table 1: Priors for the Model Parameters			
Parameter	Prior	Parameter	Prior
λ_{20K}^{τ}	$N(1, 0.1)$	λ_{20K}^{π}	$N(-4, 1)$
λ_{40K}^{τ}	$N(1, 0.1)$	λ_{40K}^{π}	$N(-2, 1)$
λ_{100K}^{τ}	$N(1, 0.1)$	λ_{100K}^{π}	$N(0, 1)$
λ_{200K}^{τ}	$N(1, 0.1)$	λ_{200K}^{π}	$N(2, 1)$
λ_{400K}^{τ}	$N(1, 0.1)$	λ_{400K}^{π}	$N(4, 1)$
λ_{1M}^{τ}	$N(1, 0.1)$	λ_{1M}^{π}	$N(8, 1)$
σ_i^2	$IG(6, 0.001)$		
Structural VAR Parameters:			Prior
Overall tightness of prior beliefs			$\lambda_0 = \frac{1}{\sqrt{0.001}}$
Tightens the prior around zero for coefficients on lags of other variables			$\lambda_1 = 0.2$
Controls the rate at which the prior tightens as the lag length increases			$\lambda_3 = 1$
Controls the tightness of the coefficient on the linear trend			$\lambda_4 = 10$

Table 1: Priors for the Model Parameters: N is the number of variables in the VAR and m is the number of parameters for each lag of the VAR

Table 2: Variance Decompositions			
Income Level	Level	Progressivity	Idiosyncratic
$20,000	0.44	0.03	0.54
$40,000	0.83	0.06	0.11
$100,000	0.67	0.04	0.28
$200,000	0.91	0.02	0.07
$400,000	0.80	0.20	0.00
$1,000,000	0.65	0.28	0.07

Table 2: Variance decompositions computed based on the tax level and progressivity factors produced from the FAVAR model
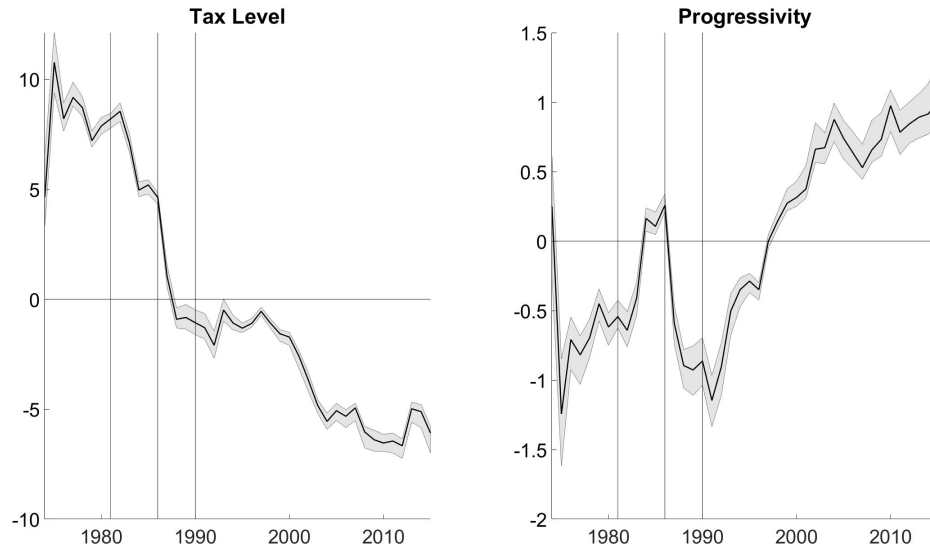

Figure 1: Posterior distribution of the tax level and progressivity factors extracted from observed tax data in the FAVAR model. The solid line and light shaded region depict the median and 68% posterior coverage of the estimated factors across Gibbs draws.
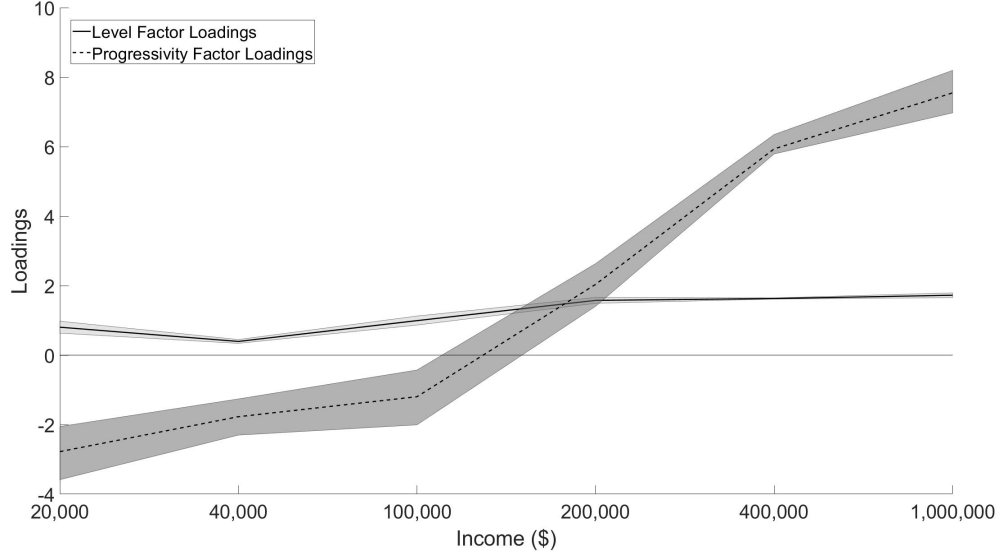
Figure 2: Posterior distribution of the factor loadings estimated from FAVAR model. The solid line and light shaded region depict the median and 68% posterior coverage of the estimated level factor loadings. The dashed line and dark shaded region depict the median and 68% posterior coverage of the estimated progressivity factor loadings.
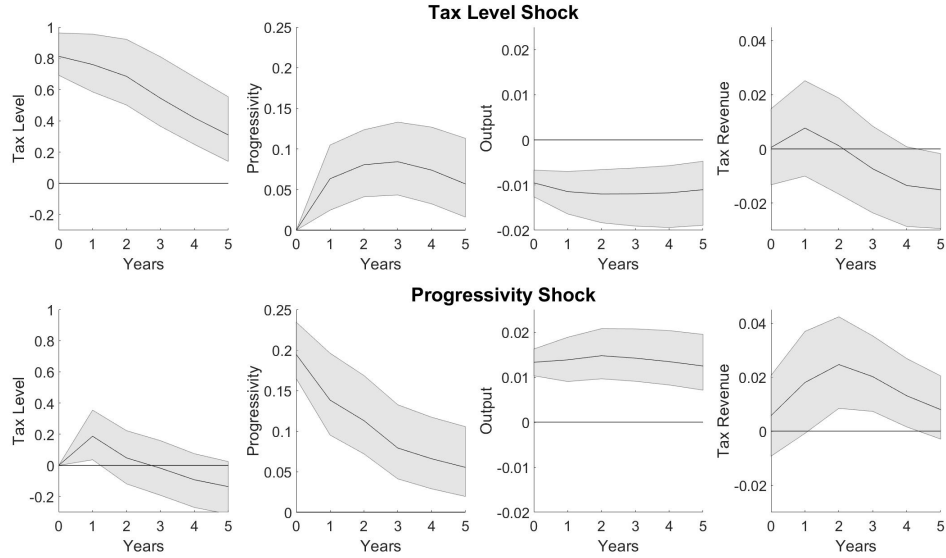

Figure 3: Impulse responses to tax shocks from the baseline FAVAR with the tax level factor, tax progressivity factor, log real GDP, and log real tax revenue. The top row depicts the responses to a tax level shock while the bottom row shows the responses to a progressivity shock. The solid line and shaded region represent the posterior median and 68% posterior coverage across all Gibbs draws.
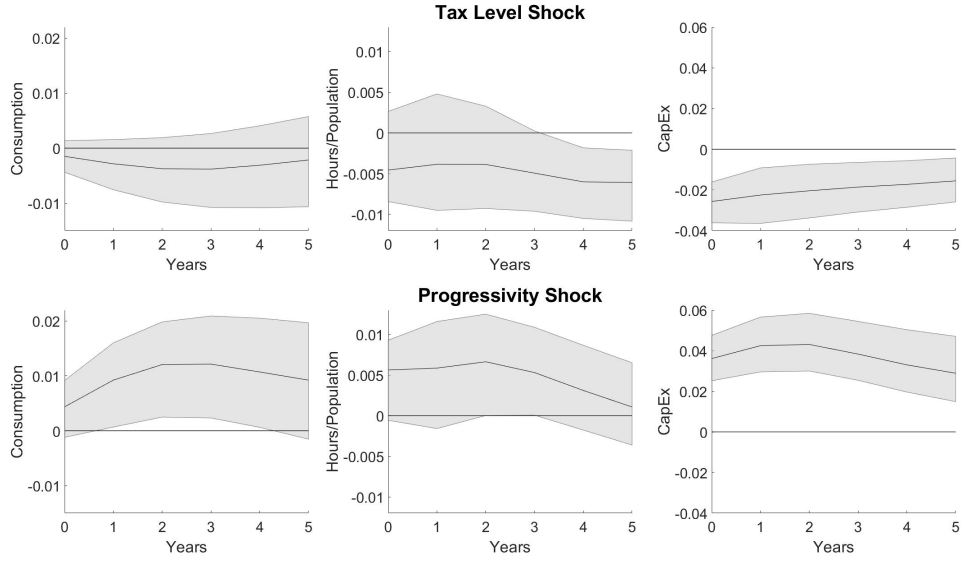
Figure 4: Impulse responses from the FAVAR with (i) the tax level factor, tax progressivity factor, log real consumption expenditure, and log real tax revenue; (ii) the tax level factor, tax progressivity factor, log real GDP, log real tax revenue, and log hours/population, and (iii) the tax level factor, tax progressivity factor, log CapEx $, and log real tax revenue. The top row depicts the responses to a tax level shock while the bottom row shows the responses to a progressivity shock. The solid line and shaded region represent the posterior median and 68% posterior coverage across all Gibbs draws.
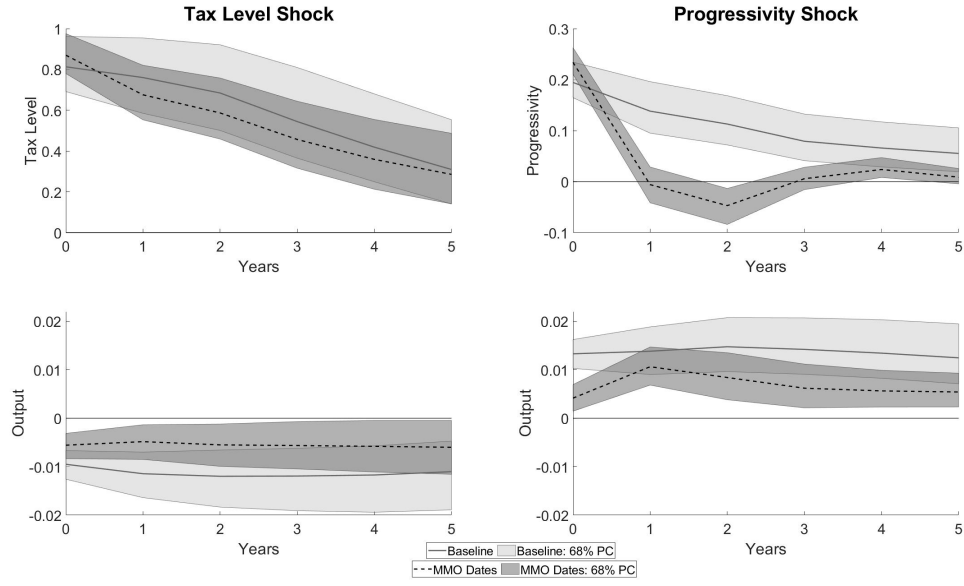
Figure 5: Impulse responses from the FAVAR with (i) the tax level factor, tax progressivity factor, log real GDP, and log real tax revenue; (ii) the tax level factor, tax progressivity factor dummied out to include only the dates identified by the narrative approach in Mertens and Montiel Olea (2018), log real GDP, and log real tax revenue. The solid line and shaded region represent the posterior median and 68% posterior coverage across all Gibbs draws.
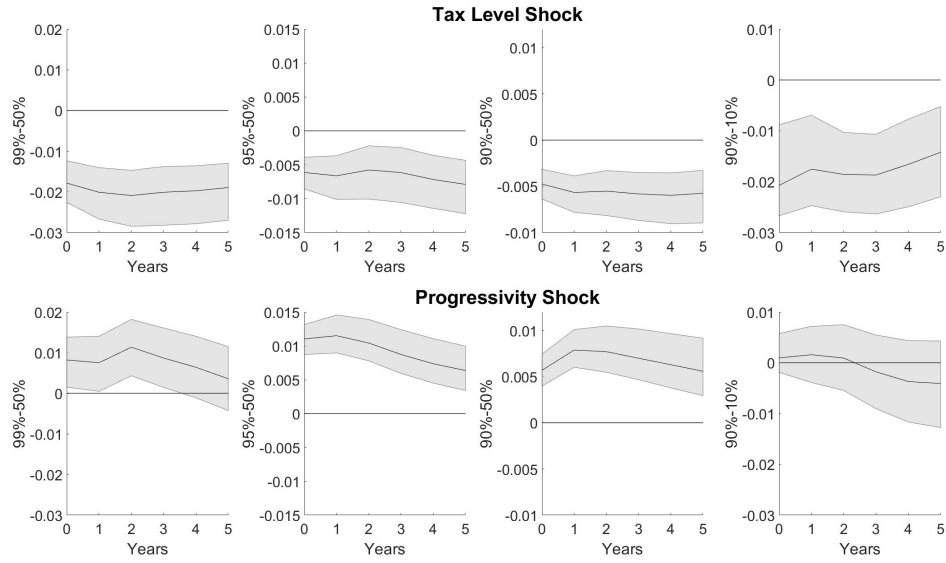
Figure 6: Impulse responses from the FAVAR with the tax level factor, tax progressivity factor, log real tax revenue, and various measures of income inequality from Piketty, Saez and Zucman (2018). The top row depicts the responses to a tax level shock while the bottom row shows the responses to a progressivity shock. The solid line and shaded region represent the posterior median and 68% posterior coverage across all Gibbs draws.
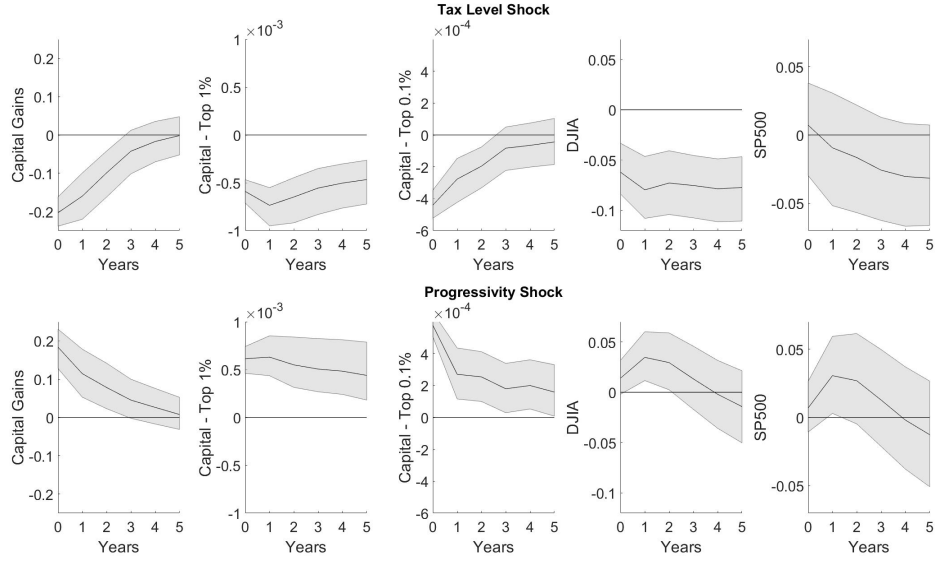
Figure 7: Responses to level and progressivity shocks from the FAVAR with the tax level factor, tax progressivity factor, log real tax revenue, and one of the following measures: (i) log real total realized capital gains; (ii) capital income share of the top 1%; (iii) capital income share of the top 0.1%; (iv) log DJIA Index; (v) log SP500. The top row depicts the responses to a tax level shock while the bottom row shows the responses to a progressivity shock. The solid line and shaded region represent the posterior median and 68% posterior coverage across all Gibbs draws.
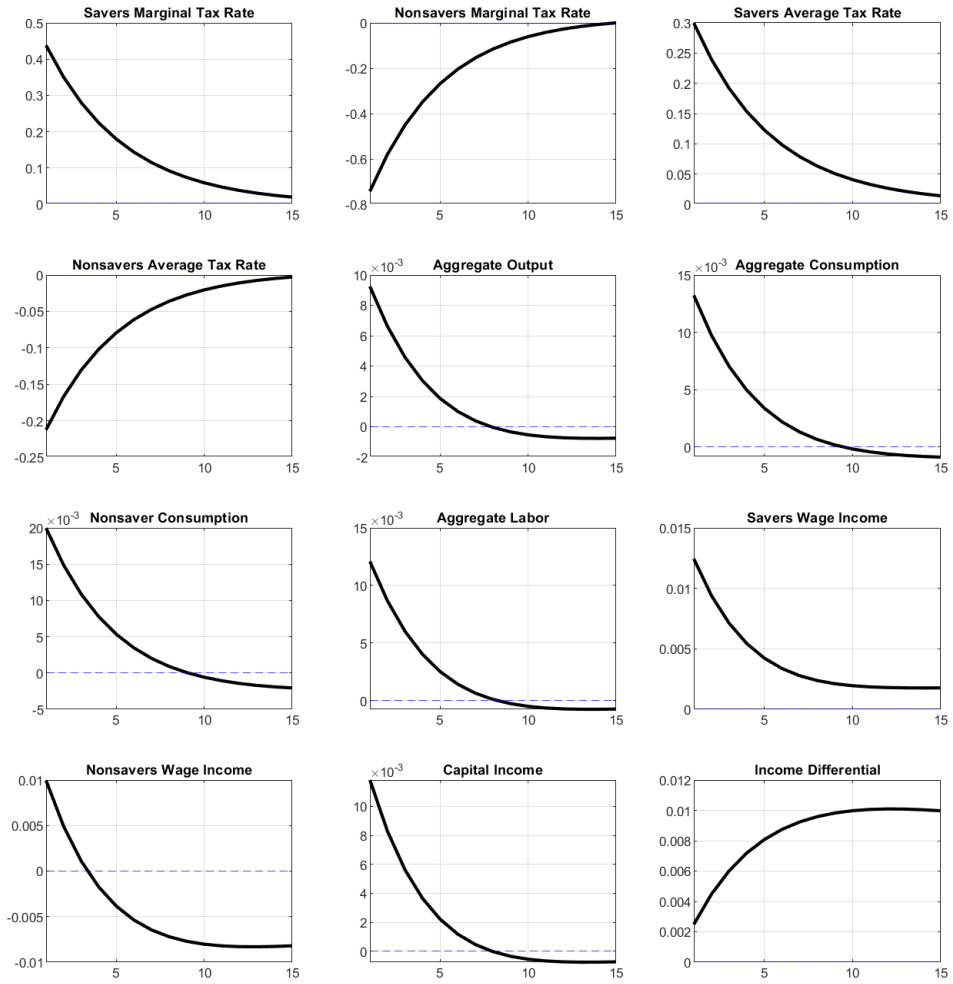
Figure 8: Impulse responses in the TANK model following unanticipated increase in tax progressivity to savers.
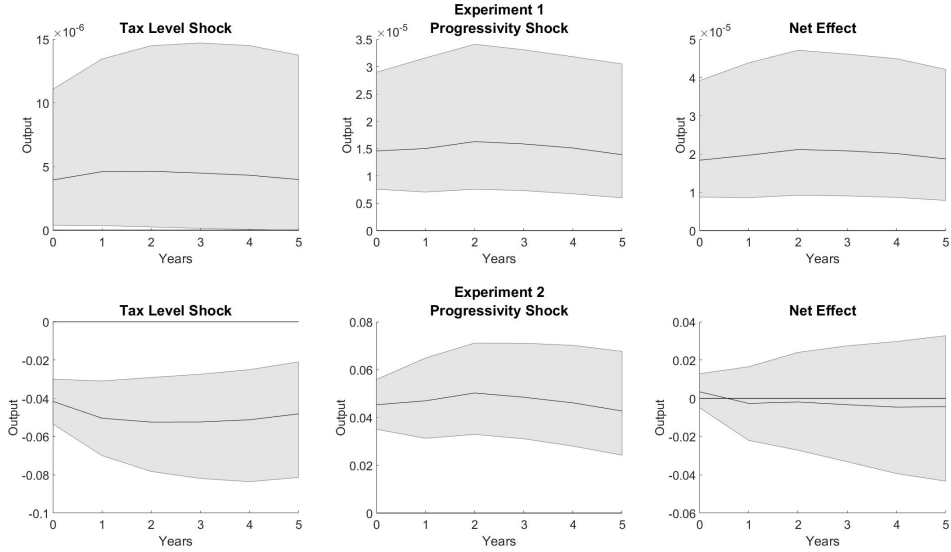
Figure 9: Impulse responses from the two policy experiments. In Experiment 1, the tax rate on the highest incomes, over $1 million, is increased by 0.1. In Experiment 2, the tax rate on the two highest incomes, over $400,000 and over $1 million, are increased by 0.1. We conduct the experiment using draws of the model parameters across all Gibbs iterations and plot the median and 68% posterior coverage.
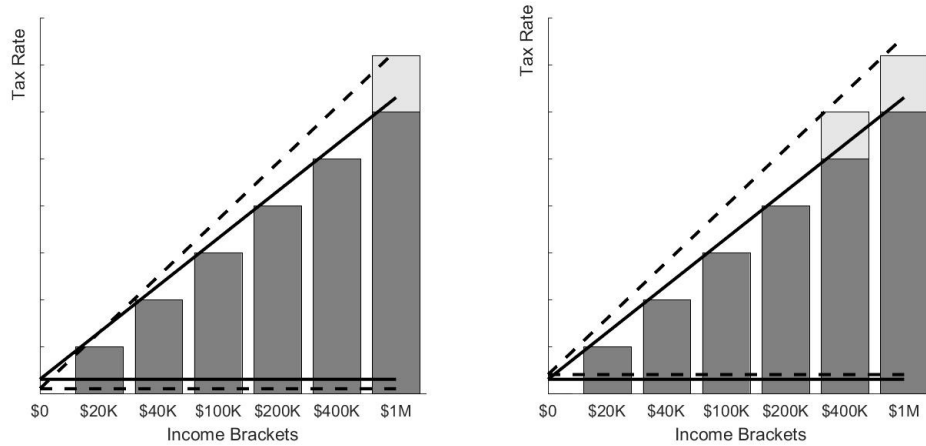

Figure 10: Graphical representation of the policy experiments and the effects on the tax level and progressivity factors.The top row shows Experiment 1 in which the tax rate on the highest incomes, over $1 million, is increased by 0.1. The bottom row shows Experiment 2 in which the tax rate on the two highest incomes, over $400,000 and over $1 million, are increased by 0.1.

A Details of the Structural VAR Estimation

A.1 The Prior

Denote a_i and b_i as the ith columns of $\mathbf{A}_0'$ and $\mathbf{A}'$, respectively. This allows one to consider each equation of the structural VAR separately, as in Waggoner and Zha (2003). We utilize a variation of the prior proposed by Sims and Zha (1998). This prior imposes independence across structural equations and thus imposes a prior on the elements of a_i to be jointly normal and mean zero. Additionally, the prior of b_i is conditional on a_i. Following the general framework of the prior described in Litterman (1986), Sims and Zha (1998) impose that the conditional mean of the coefficients in b_i on the first lag term in the VAR is equal to a_i, while the coefficients on the remaining lags have mean zero. In doing so, this assumes that the random walk is a reasonable approximation of the behavior of the variables within the VAR. In our VAR, we include the factors, log real GDP, and log real tax revenue. As discussed in Litterman (1986), if the variables within the VAR must be stationary, it may be more appropriate to specify a prior assuming less persistence. Additionally, we wish to assign some meaningful role to the factors without violating stationarity of the transition equation in the state-space system.[38] Furthermore, since we incorporate a linear trend component to the dynamics of the VAR, these should also be stationary. To accomplish this, we set the prior such as to impose the mean of the reduced-form coefficient in each equation on their own first lag is centered around 0. Ultimately, the prior on the VAR coefficients can be described as the following:

$$a_i \sim N\left(0, \overline{S}_i\right),$$

$$b_i | a_i \sim N\left(\overline{P}_i a_i, \overline{H}_i\right),$$

for $i = 1, ..., N + K$.

Sims and Zha (1998) define a set of hyperparameters to control the tightness of various components of the prior. We adopt a subset of these hyperparameters necessary to implement the prior in our specification of the structural VAR model. These are defined in Table **2**.

---

[38]This stability is important for the Kalman filter step in which we estimate the factors.

We construct $\overline{S}_i$ as a diagonal matrix with the standard deviation for coefficients on elements in the jth row of the VAR defined as $\frac{\lambda_0}{\sigma_j}$. The σ_j terms are scale factors that account for potential variation in the units of measure of the data. Thus, σ_j^2 is computed as the sample variance of residuals from univariate autoregressions.

As discussed previously, we adjust the prior on the first lag to be zero. The matrix $\overline{P}_i$ consists of $diag\left[0_{1 \times K+N}\right]$ in the first $N + K$ rows and zeros elsewhere, corresponding to all coefficients on lags greater than 1. We construct $\overline{H}_i$ as a diagonal matrix with the variance of coefficients on the kth lag of variable j as $\frac{\lambda_0^2 \lambda_1^2}{\sigma_j^2 k^{\lambda_3}}$.

A.2 Drawing $\mathbf{A}_0$ and $\mathbf{A}|\mathbf{A}_0$ conditional on $\Psi_{-\mathbf{A}_0}$

To implement the draw for each of these columns, define c_i and d_i such that $a_i = U_i c_i$ and $b_i = V_i d_i$, where U_i and V_i are orthonormal rotation matrices that impose the identifying restrictions placed upon $\mathbf{A}_0$ and $\mathbf{A}$. Considering the normal prior for a_i and b_i, the marginal posterior pdf of c_i and d_i take the form:

$$p\left(c_1, ..., c_{N+K} | \widetilde{Y}_T, \widetilde{X}_T, \widetilde{Z}_T\right) \propto \left|\det\left[U_1 c_1 |...| U_{N+K} c_{N+K}\right]\right|^T \exp\left(-\frac{T}{2} \sum_{i=1}^{N+K} c_i' S_i^{-1} c_i\right) \qquad (4)$$

$$p\left(d_i | c_i, \widetilde{Y}_T, \widetilde{X}_T, \widetilde{Z}_T\right) = \phi\left(P_i c_i, H_i\right), \qquad (5)$$

where H_i, P_i, S_i are the parameters of the posterior based upon the transformations described in Waggoner and Zha (2003) and ϕ is the pdf of the Normal distribution with mean $P_i c_i$ and variance H_i. The Gibbs sampler sequentially draws each c_i, conditional on the other c_j, $j = 1, ..., i - 1, i + 1, ..., N + K$. Once we obtain a draw for c_i, and thus a_i, we use (5) to draw d_i and compute b_i. Upon completion of the draws for a_i and b_i $\forall i$, we construct the matrices $\mathbf{A}_0$ and $\mathbf{A}$ and convert them to the reduced-form expressions $B = \mathbf{A}_0^{-1}\mathbf{A}$ and $\Omega = (\mathbf{A}_0'\mathbf{A}_0)^{-1}$ for use in the Kalman filter.

B TANK Model

The model is a two-agent New Keynesian model. Households consist of agents who can save and agents who are constrained to consume their income each period. We assume that each type of agent supplies their own type of labor. Production depends on capital and both types of labor inputs. Labor income is subject to a progressive income tax. The monetary authority follows a standard Taylor rule.

B.1 Households

The economy is populated by a continuum of households on the interval $[0, 1]$, of which a fraction μ are nonsavers. These households do not have access to financial or capital markets and consume all of their disposable income each period. The remaining $(1 - \mu)$ fraction of households are forward-looking with access to asset and capital markets. The superscript s indicates a variable associated with savers and n with nonsavers. We allow for imperfect substitutability of labor inputs of savers and non-savers, which implies each labor type is subject to its own wage rate.

Savers. The jth saver maximizes utility, given by

$$E_0 \sum_{t=0}^{\infty} \beta^t \left[\frac{(c_t^s(j) - \theta_s c_{t-1}^s)^{1-\gamma_s} - 1}{1 - \gamma_s} - \chi^s \frac{l_t^s(j)^{1+\kappa_s}}{1 + \kappa_s} \right], \tag{6}$$

where $\beta \in (0, 1)$ is the savers' discount factor, $\gamma_s \geq 0$ measures risk aversion, and $\kappa_s \geq 0$ is the inverse of the Frisch labor elasticity.

At time t, household j purchases $b_t^S(j)$ units of government debt, which pays $\frac{R_t b_t^S(j)}{\pi_{t+1}}$ units of consumption goods at $t+1$, where $\Pi_{t+1} \equiv \frac{P_{t+1}}{P_t}$ is the gross inflation rate for the consumer price index. Labor income, $Inc_t^s(j) \equiv w_t^s(j) l_t^s(j)$, is subject to an income tax. Let τ_t^s denote the income tax rate, which is given by the function[39]

$$\tau_t^s = 1 - \xi_t \left(Inc_t^s(j) \right)^{-\phi_t}.$$

---

[39]This tax function was first proposed by Feldstein (1969) and has been widely used in the literature.

$1 - \xi_t$ represents a flat-level component to the tax schedule (i.e., the rate that would prevail without progressivity), while ϕ_t is a progressivity component. The marginal tax rate is given by

$$\tau_t^{m,s} \equiv \frac{\partial \tau_t^s Inc_t^s(j)}{\partial Inc_t(j)} = 1 - \xi_t(1 - \phi_t) \left(Inc_t^s(j)\right)^{-\phi_t}. \tag{7}$$

Households have some monopoly power in setting their wage rate, $w_t^s(j)$. We assume that wage adjustments are subject to a Rotemberg-type quadratic adjustment cost. In addition, the household receives capital income, $r_t^K u_t(j) k_{t-1}^s(j)$. Capital has a variable utilization rate $u_t(j)$, which incurs a real cost of $\psi(u_t(j)) k_{t-1}^s(j)$ to vary.

The flow budget constraint in units of consumption goods for the jth saver is given by

$$
\begin{aligned}
(1 - \tau_t^s) Inc_t^s(j) + \frac{R_{t-1} b_{t-1}^s(j)}{\Pi_t} + d_t^s(j) + z_t^s(j) = \\
c_t^s(j) + i_t^s(j) + b_t^s(j) + \psi(u_t(j)) k_{t-1}^s(j) + \frac{\Phi_w^s}{2} \left(\frac{w_t^s(j)}{w_{t-1}^s(j)} \frac{\Pi_t}{\Pi} - 1 \right)^2 Y_t,
\end{aligned}
\tag{8}
$$

where $d_t^S(j)$ is dividends received from profits of the monopolistic firms, $i_t^S(j)$ is gross investment, and $z_t^s(j)$ is a lump-sum transfer/tax.

The law of motion for capital is

$$k_t^s(j) = \left[1 - \frac{\chi}{2} \left(\frac{i_t^s(j)}{i_{t-1}^s(j)} - 1 \right)^2 \right] i_t^s(j) + (1 - \delta) k_{t-1}^s(j).$$

We assume that capital utilization in steady state is 1 and that the costs for varying utilization take the form

$$\psi(u_{t+1}(j)) = \psi_1[u_{t+1}(j) - 1] + \frac{\psi_2}{2}[u_{t+1}(j) - 1]^2.$$

Nonsavers. We assume nonsavers have the same preferences as savers. Nonsavers have no access to asset markets. However, they do have an intertemporal choice in that they have monopoly power in setting their wage rate, $w_t^n(j)$ The budget constraint of the jth nonsaver is

$$c_t^n(j) = (1 - \tau_t^n) w_t^n(j) l_t^n(j) + z_t^n(j) + \frac{\Phi_w^n}{2} \left(\frac{w_t^n(j)}{w_{t-1}^n(j)} \frac{\Pi_t}{\Pi} - 1 \right)^2 Y_t,$$

where z_t^n represents a transfer from the government, and the income tax function is given by

$$\tau_t^n \equiv 1 - \xi_t \left(w_t^n(j) l_t^n(j) \right)^{-\phi_t} .$$

The marginal tax rate for nonsavers is

$$\tau_t^{m,n} \equiv 1 - \xi_t (1 - \phi_t) \left(w_t^n(j) l_t^n(j) \right)^{-\phi_t} .$$

B.2 Labor Aggregation

A perfectly competitive labor packer purchases the differentiated labor inputs and assembles them to produce composite labor services L_t^s and L_t^n according to the CES technology:

$$L_t^s = \left[\left(\frac{1}{1-\mu} \right)^{\frac{1}{\theta_w^s}} \int_\mu^1 l_t^s(l)^{\frac{\theta_w^s - 1}{\theta_w^s}} dl \right]^{\frac{\theta_w^s}{\theta_w^s - 1}} , L_t^n = \left[\left(\frac{1}{\mu} \right)^{\frac{1}{\theta_w^n}} \int_0^\mu l_t^n(l)^{\frac{\theta_w^n - 1}{\theta_w^n}} dl \right]^{\frac{\theta_w^n}{\theta_w^n - 1}} \tag{9}$$

where θ_w^s and θ_w^n denote markups to wages. Maximization implies the wage indexes:

$$W_t^s = \left[\left(\frac{1}{1-\mu} \right) \int_\mu^1 W_t^s(j)^{1-\theta_w^s} dj \right]^{\frac{1}{\theta_w^s - 1}} , W_t^n = \left[\left(\frac{1}{\mu} \right) \int_0^\mu W_t^n(j)^{1-\theta_w^n} dj \right]^{\frac{1}{\theta_w^n - 1}} \tag{10}$$

B.3 Firms and Price Setting

The production sector consists of intermediate and final goods producing firms. A perfectly competitive final goods producer uses a continuum of intermediate goods $y_t(i)$, where $i \in [0, 1]$, to produce the final good, Y_t, according to the constant-return-to-scale technology

$$Y_t = \left[\int_0^1 y_t(i)^{\frac{\theta_p - 1}{\theta_p}} di \right]^{\frac{\theta_p}{\theta_p - 1}} . \tag{11}$$

where $\theta_p > 1$ is the price elasticity of demand. We denote the price of good i as $p_t(i)$, and the price of the final good Y_t as P_t.

The final good producing firm chooses Y_t and $y_t(i)$ to maximize profits subject to the

technology (11). The demand for $y_t(i)$ is given by

$$y_t(i) = \left[\frac{p_t(i)}{P_t}\right]^{-\theta_p} Y_t. \tag{12}$$

Maximization implies the aggregate price index

$$P_t = \left[\int_0^1 p_t(i)^{1-\theta} di\right]^{\frac{1}{1-\theta_p}}. \tag{13}$$

Intermediate goods producers, indexed by i, are monopolistic competitors in their product market and take production factor prices as given. Firm i produces by a Cobb-Douglas technology

$$y_t(i) = (u_t(i)k_{t-1})(i)^\alpha l_t(i)^{1-\alpha}, \tag{14}$$

where $\alpha \in [0,1]$. k_t is equivalent to effective capital $k_{t-1}u_t$. l_t represents the total amount of composite labor, which is a constant-elasticity-of-substitution (CES) aggregate of each household's labor type:

$$l_t = \left[(1-\varphi)^{-\frac{1}{\eta}}(L_t^s)^{\frac{1+\eta}{\eta}} + \varphi^{-\frac{1}{\eta}}(L_t^n)^{\frac{1+\eta}{\eta}}\right]^{\frac{\eta}{1+\eta}} \tag{15}$$

where $\eta > 0$ is the intratemporal elasticity of substitution between labor types and φ is the steady-state share of composite labor worked by nonsavers.

Price adjustments are subject to quadratic adjustment costs, measured in units of the final good, similar to Rotemberg (1982):

$$\frac{\Phi_p}{2}\left(\frac{p_t(i)}{\bar{\Pi}p_{t-1}(i)} - 1\right)^2 Y_t.$$

where $\Phi_p > 0$ determines the magnitude of the cost and $\bar{\Pi}$ denotes gross steady-state inflation. Optimization gives the Phillips curve

$$\left[(1-\theta_p) + \theta_p mc_t - \Phi_p\frac{\Pi_t}{\bar{\Pi}}\left(\frac{\Pi_t}{\bar{\Pi}} - 1\right)\right] + \Phi_p\beta E_t\frac{\lambda_{t+1}^s}{\lambda_t^s}\frac{Y_{t+1}}{Y_t}\frac{\Pi_{t+1}}{\bar{\Pi}}\left(\frac{\Pi_{t+1}}{\bar{\Pi}} - 1\right) = 0, \tag{16}$$

where mc_t denotes real marginal costs.

B.4 Monetary and Fiscal Policy

The monetary authority follows a Taylor-type rule, given by

$$\frac{R_t}{R} = \left(\frac{R_{t-1}}{R}\right)^{\rho_r} \left[\left(\frac{\Pi_t}{\Pi}\right)^{\phi_\pi} \left(\frac{Y_t}{Y}\right)^{\phi_y}\right]^{1-\rho_r}$$

The government budget constraint is

$$g_t + z_t^n + z_t^s + \frac{R_{t-1}b_{t-1}}{\pi_t} = b_t + \mu\tau_t^n w_t^n L_t^n + (1-\mu)\tau_t^s(w_t^s L_t^s)$$

We assume that public spending and transfers to nonsavers are exogenously set by the government. Ricardian equivalence holds as transfers to savers adjust to satisfy the government budget constraint.

Policy Experiment. To replicate the twist to tax progressivity implied by the empirical estimates, we allow the tax function parameters to vary with the type of agent. Specifically, we assume that there is an exogenous shock that increases the tax progressivity of savers:

$$\ln\left(\frac{\phi_t^s}{\phi}\right) = \rho_\phi \ln\left(\frac{\phi_{t-1}^s}{\phi}\right) + \epsilon_t^\phi, \quad \epsilon_t^\phi \sim N(0,1).$$

At the same time, the flat-level component ξ_t^s remains constant. To ensure that the policy remains revenue neutral, we additionally assume that the progressivity parameter of nonsavers (ϕ_t^n) is endogenously adjusted so that:

$$\mu\tau_t^n w_t^n L_t^n + (1-\mu)\tau_t^s(w_t^s L_t^s) = \mu\tau^n w^n L^n + (1-\mu)\tau^s(w^s L^s.$$

B.5 Aggregation

Aggregate consumption is

$$c_t = \mu c_t^n + (1-\mu)c_t^s$$

The resource constraint is

$$Y_t = c_t + i_t + g_t + \frac{\Phi_p}{2}\left(\frac{\Pi_t}{\bar{\Pi}} - 1\right)^2 Y_t + \psi(u_t)k_{t-1} + \frac{\Phi_w^n}{2}\left(\frac{w_t^n}{w_{t-1}^n}\frac{\Pi_t}{\Pi} - 1\right)^2 Y_t + \frac{\Phi_w^s}{2}\left(\frac{w_t^s}{w_{t-1}^s}\frac{\Pi_t}{\Pi} - 1\right)^2 Y_t$$

C Equilibrium Conditions

$$k_t = \left[1 - \frac{\chi}{2}\left(\frac{i_t}{i_{t-1}} - 1\right)^2\right] i_t + (1-\delta)k_{t-1} \tag{17}$$

$$q_t = \beta E_t \frac{\lambda_{t+1}^s}{\lambda_t^s}\left\{r_{t+1}^K u_{t+1} - \psi(u_{t+1}) + (1-\delta)q_{t+1}\right\} \tag{18}$$

$$r_t^k = \psi_1 + \psi_2[u_{t+1} - 1] \tag{19}$$

$$\lambda_t^s = (c_t^s - \theta_s c_{t-1}^s)^{-\gamma_s} \tag{20}$$

$$\lambda_t^s = \beta E_t \frac{R_t \lambda_{t+1}^s}{\Pi_{t+1}} \tag{21}$$

$$1 = q_t\left[1 - \frac{\chi}{2}\left(\frac{i_t}{i_{t-1}} - 1\right)^2 - \chi\left(\frac{i_t}{i_{t-1}} - 1\right)\frac{i_t}{i_{t-1}}\right] + \beta E_t \frac{\lambda_{t+1}^s}{\lambda_t^s}q_{t+1}\chi\left(\frac{i_{t+1}}{i_t} - 1\right)\left(\frac{i_{t+1}}{i_t}\right)^2 \tag{22}$$

$$\frac{\Phi_w^s}{2}\left(\frac{w_t^s}{w_{t-1}^s}\frac{\Pi_t}{\bar{\Pi}} - 1\right)\frac{w_t^s}{w_{t-1}^s}\frac{\Pi_t}{\bar{\Pi}}Y_t =$$
$$\beta E_t \frac{\lambda_{t+1}}{\lambda_t}\frac{\Phi_w^s}{2}\left(\frac{w_{t+1}^s}{w_t^s}\frac{\Pi_{t+1}}{\bar{\Pi}} - 1\right)\frac{w_{t+1}^s}{w_t^s}\frac{\Pi_{t+1}}{\bar{\Pi}}Y_{t+1} + \theta_w^s\chi^s\frac{(L_t^s)^{1+\kappa_s}}{\lambda_t} + (1-\theta_w^s)(1-\tau_t^{m,s})L_t^s w_t^s \tag{23}$$

$$\frac{\Phi_w^n}{2}\left(\frac{w_t^n}{w_{t-1}^n}\frac{\Pi_t}{\bar{\Pi}} - 1\right)\frac{w_t^n}{w_{t-1}^n}\frac{\Pi_t}{\bar{\Pi}}Y_t =$$
$$\beta E_t \frac{\lambda_{t+1}}{\lambda_t}\frac{\Phi_w^n}{2}\left(\frac{w_{t+1}^n}{w_t^n}\frac{\Pi_{t+1}}{\bar{\Pi}} - 1\right)\frac{w_{t+1}^n}{w_t^n}\frac{\Pi_{t+1}}{\bar{\Pi}}Y_{t+1} + \theta_w^n\chi^n\frac{(L_t^n)^{1+\kappa_n}}{(c_t^n - \theta_n c_{t-1}^n)^{-\gamma_n}} + (1-\theta_w^n)(1-\tau_t^{m,n})L_t^n w_t^n \tag{24}$$

$$\tau_t^{m,s} = 1 - \xi_t^s(1 - \phi_t^s)\left(L_t^s w_t^s\right)^{-\phi_t^s} \tag{25}$$

$$\tau_t^s = 1 - \xi_t^s\left(L_t^s w_t^s\right)^{-\phi_t^s} \tag{26}$$

$$\tau_t^n \equiv 1 - \xi_t^n \left(w_t^n L_t^n \right)^{-\phi_t^n} \tag{27}$$

$$\tau_t^{m,n} \equiv 1 - \xi_t^n (1 - \phi_t^n) \left(w_t^n L_t^n \right)^{-\phi_t^n} \tag{28}$$

$$c_t^n = (1 - \tau_t^n) w_t^n L_t^n + z_t^n + \frac{\Phi_w^n}{2} \left(\frac{w_t^n}{w_{t-1}^n} \frac{\Pi_t}{\Pi} - 1 \right)^2 Y_t \tag{29}$$

$$\hat{L}_t^n = \hat{L}_t^s \tag{30}$$

$$c_t = \mu c_t^n + (1 - \mu) c_t^s \tag{31}$$

$$Y_t = (u_t k_{t-1})^\alpha L_t^{1-\alpha}, \tag{32}$$

$$L_t = \left[(1 - \varphi)^{-\frac{1}{\eta}} \left(L_t^s \right)^{\frac{1+\eta}{\eta}} + \varphi^{-\frac{1}{\eta}} \left(L_t^n \right)^{\frac{1+\eta}{\eta}} \right]^{\frac{\eta}{1+\eta}} \tag{33}$$

$$r_t^k = mc_t \alpha \frac{Y_t}{k_{t-1} u_t} \tag{34}$$

$$w_t^n = mc_t(1 - \alpha) \frac{Y_t}{L_t} \varphi^{-\frac{1}{\eta}} L_t^{\frac{-1}{\eta}} \left(L_t^n \right)^{\frac{1}{\eta}} \tag{35}$$

$$w_t^s = mc_t(1 - \alpha) \frac{Y_t}{L_t} (1 - \varphi)^{-\frac{1}{\eta}} l_t^{\frac{-1}{\eta}} \left(L_t^s \right)^{\frac{1}{\eta}} \tag{36}$$

$$\left[(1 - \theta_p) + \theta_p mc_t - \Phi_p \frac{\Pi_t}{\bar{\Pi}} \left(\frac{\Pi_t}{\bar{\Pi}} - 1 \right) \right] + \Phi_p \beta E_t \frac{\lambda_{t+1}^s}{\lambda_t^s} \frac{Y_{t+1}}{Y_t} \frac{\Pi_{t+1}}{\bar{\Pi}} \left(\frac{\Pi_{t+1}}{\bar{\Pi}} - 1 \right) = 0 \tag{37}$$

$$Y_t = c_t + i_t + g_t + \frac{\Phi_p}{2} \left(\frac{\Pi_t}{\bar{\Pi}} - 1 \right)^2 Y_t + \psi(u_t) k_{t-1} + \frac{\Phi_w^n}{2} \left(\frac{w_t^n}{w_{t-1}^n} \frac{\Pi_t}{\Pi} - 1 \right)^2 Y_t + \frac{\Phi_w^s}{2} \left(\frac{w_t^s}{w_{t-1}^s} \frac{\Pi_t}{\Pi} - 1 \right)^2 Y_t \tag{38}$$

$$\frac{R_t}{R} = \left(\frac{R_{t-1}}{R} \right)^{\rho_r} \left[\left(\frac{\Pi_t}{\Pi} \right)^{\phi_\pi} \left(\frac{Y_t}{Y} \right)^{\phi_y} \right]^{1-\rho_r} \tag{39}$$

$$g_t + z_t^n + z_t^s + \frac{R_{t-1} b_{t-1}}{\pi_t} = b_t + \mu \tau_t^n w_t^n L_t^n + (1 - \mu) \tau_t^s (w_t^s L_t^s) \tag{40}$$

D   Calibration

Table 3 gives our calibration. The tax parameters are calibrated as in Chen and Guo (2013), which are based on estimates for the U.S. tax function and consistent with estimates from other studies. We assume that in steady state, savers work half as much as non-savers while

they consume twice as much consumption. The large share of nonsavers helps replicate the empirical estimates, where only the top 3 tax brackets experience an increase in tax rates. Given the rest of the calibration, the tax function implies that in steady state, the average tax rates are $\tau^s = 0.29$ and $\tau^n = 0.23$ and the marginal tax rates are $\tau^{m,s} = 0.38$ and $\tau^{m,n} = 0.33$.

We set the price adjustment cost to a value that would replicate the frequency of price adjustment in a Calvo-type Phillips curve in the absence of strategic price complementarities, specifically to match an average duration of 4 quarters. Likewise, we set the wage adjustment cost to a value that would replicate the frequency of wage adjustment in a Calvo-type wage Phillips curve, to match an average duration of 4 quarters.[40]

Table 3: Calibration

Intertemporal Elasticity of Substitution	$\gamma_s = \gamma_n = 1$	Discount Factor	$\beta = 0.99$
Steady state nonsaver labor	$\bar{L}^N = 2$	Steady state saver labor	$\bar{L}^S = 1$
Price elasticity of demand	$\theta_p = 6.25$	Depreciation of capital	$\bar{\delta} = 0.025$
Rotemberg adjustment cost	$\Phi_p = 61.165$	Gov. spending to GDP ratio	$\frac{\bar{G}}{\bar{Y}} = 0.15$
Flat tax parameter	$\xi^s = \xi^n = 0.8$	Progressive tax parameter	$\phi^s = \phi^n = 0.13$
Taylor rule inflation response	$\phi_\pi = 1.25$	Taylor rule output response	$\phi_y = 0.1$
Taylor rule interest response	$\rho_r = 0.8$	Investment adjustment costs	$\chi = 8$
Fraction of nonsavers	$\mu = \varphi = 0.8$	Persistence of shocks	$\rho_x = 0.8$
Capital share	$\alpha = 0.3$	Habit for consumption	$\theta_s = 0.75$
Utilization costs	$\psi_2 = 5.67$	Elasticity of labor substitution	$\eta = 0.5$
Inverse Frisch Elasticity of Labor Supply	$\kappa_n = \kappa_s = 0.2$		

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[40]While the duration is the same across savers and nonsavers, the implied wage adjustment costs, Φ_w^n and Φ_w^s, differ, due to differences in the steady-state wages and labor of savers and nonsavers.